



Chapter \_\_\_\_\_ : \_\_\_\_\_

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## 11.1 Arithmetic Sequences

### nth Term of an Arithmetic Sequence

You can use the formula to find a term in a sequence given the first term and the common difference OR given the first term and some successive terms.

#### **Example 1: Find a Particular Term**

Find the indicated term of each arithmetic sequence.

a)  $a_1 = -4$ ,  $d = -9$ ,  $n = 20$

b)  $a_{12}$  for 8, 3, -2,...

- c) The table below shows typical costs for a construction company to rent a crane for 1-4 months. If the sequence continues, will the company be able to afford the crane rental for a job that is expected to last 18 months if they have a budget of \$350,000 for crane rental?

Months	Cost (\$)
1	75,000
2	90,000
3	105,000
4	120,000

#### **Example 2: The nth Term**

- a) Write an equation for the nth term of the arithmetic sequence: -26, -15, -4, 7,....

- b) Complete: 68 is the \_\_\_\_th term of the arithmetic sequence -2, 3, 8,...

#### **Example 3: Find Arithmetic Means**

→ the terms between any two nonsuccessive terms of an arithmetic sequence

Find the arithmetic means in each sequence.

a) 10, \_\_\_\_, \_\_\_\_, -8

b) 3, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_, 27

## 11.2 Arithmetic Series

### Sum of an Arithmetic Series

#### Example 1: Find the Sum of an Arithmetic Series

Find  $S_n$  for each arithmetic series described.

a)  $a_1 = 4$ ,  $a_n = 100$ ,  $n = 25$

b)  $a_1 = 7$ ,  $d = -2$ ,  $n = 9$

c)  $d = -3$ ,  $n = 21$ ,  $a_n = -64$

d)  $12 + 17 + 22 + \dots + 102$

#### Example 2: Find the First Three Terms

Find the first three terms of each arithmetic series described.

a)  $a_1 = 11$ ,  $a_n = 110$ ,  $S_n = 726$

b)  $n = 8$ ,  $a_n = 36$ ,  $S_n = 120$

#### Example 3: Evaluate a Sum in Sigma Notation

Find the sum of each arithmetic series.

a)  $\sum_{n=10}^{50} (3n - 1)$

b)  $\sum_{n=26}^{50} (-2n + 100)$

## 11.3 Geometric Sequences

### nth Term of a Geometric Sequence

#### **Example 1: Find Terms of a Geometric Sequence**

- a) Find the next two terms of the geometric sequence 16, 24, 36,...
- b) Find the first 5 terms of the geometric sequence:  
 $a_1 = -3$
- c) Find  $a_9$  for the geometric sequence 60, 30, 15,...
- d)  $a_4 = 16$ ,  $r = 0.5$ ,  $n = 8$
- e) An investment pays interest so that each year the value of the investment increases by 10%. How much is an initial investment of \$1000 worth after 5 years?

#### **Example 2: Write an Equation for the nth Term**

Write an equation for the nth term of the geometric sequence 18, -3,  $1/2$ ,  $-1/12$ ,...

#### **Example 3: Find Geometric Means**

Find the geometric means in each sequence.

- a) 9, \_\_\_\_, \_\_\_\_, \_\_\_\_, 144
- b) 32, \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_, 1

## 11.4 Geometric Series

### Sum of a Geometric Series

#### Example 1: Find the Sum of the First n Terms

Find  $S_n$  for each geometric series described.

a)  $a_1 = 4$ ,  $r = -3$ ,  $n = 5$

b)  $a_1 = 1296$ ,  $a_n = 1$ ,  $r = -1/6$

c)  $a_1 = 2$ ,  $a_6 = 486$ ,  $r = 3$

d)  $4096 - 512 + 64 - \dots$  to 5 terms

e) Maria arranges some rows of dominos so that after she knocks over the first one, each domino knocks over two more dominos when it falls. If there are ten rows, how many dominos does Maria use?

#### Example 2: Evaluate a Sum Written in Sigma Notation

Find the sum of each geometric series.

a)  $\sum_{n=1}^5 -4 \cdot 3^{n-1}$

b)  $\sum_{n=1}^9 5 \cdot 2^{n-1}$

#### Example 3: Find the First Term of a Series

Find the indicated term for each geometric series described.

a)  $S_n = 165$ ,  $a_n = 48$ ,  $r = -2/3$ ;  $a_1$

b)  $S_n = -364$ ,  $r = -3$ ,  $n = 6$ ;  $a_1$

## 11.5 Infinite Geometric Series

### Sum of an Infinite Geometric Series

#### Example 1: Sum of an Infinite Geometric Series

Find the sum of each infinite geometric series, if it exists.

a)  $a = 36, r = 2/3$

b)  $16 + 24 + 36 + \dots$

c) Altovese's grandfather clock is broken. When she sets the pendulum in motion by holding it against the side of the clock and letting it go, it swings 24 centimeters to the other side, then 18 centimeters back, then 13.5 centimeters, and so on. What is the total distance that the pendulum swings before it stops?

#### Example 2: Infinite Series in Sigma Notation

Find each sum of each infinite geometric series, if it exists.

a)  $\sum_{n=1}^{\infty} 6(-0.4)^{n-1}$

b)  $\sum_{n=1}^{\infty} 35\left(-\frac{3}{4}\right)^{n-1}$

#### Example 3: Write a Repeating Decimal as a Fraction

Write each repeating decimal as a fraction.

a)  $0.\overline{123}$

b)  $0.0\overline{123}$

c)  $1.\overline{234}$

## 11.6 Recursion and Special Sequences

### Recursive Formula

#### **Example 1: Use a Recursive Formula**

Find the first five terms of each sequence.

a)  $a_1 = 3, a_{n+1} = a_n + 5$

b)  $a_1 = -3, a_{n+1} = 3a_n + 2$

c)  $a_1 = 3, a_2 = 1, a_{n+1} = a_n - a_{n-1}$

d)  $a_1 = 2, a_2 = -3, a_{n+1} = 5a_n - 8a_{n-1}$

#### **Example 2: Find and Use a Recursive Formula**

Dr. Elliott is growing cells in lab dishes. She starts with 108 cells Monday morning and then removes 20 of these for her experiment. By Tuesday the remaining cells have multiplied in number by 1.5. She again removes 20. This pattern repeats each day of the week.

a) Write a recursive formula for the number of cells Dr. Elliott finds each day before she removes any.

b) How many cells will she find on Friday morning?